

# Probabilistic Failure-causing Schema in Input-Domain Testing

Ziyuan Wang    Yuanchao Qi    Jiawei Lin

School of Computer, Nanjing University of Posts and Telecommunications, Nanjing, 210003, China  
Email: wangziyuan@njupt.edu.cn

**Abstract**—To describe characteristics of failure test cases in the input-domain testing, we propose a model of probabilistic failure-causing schema. In this model, test case that contains a probabilistic failure-causing schema has a probability to be a failure test case. It may help testers to find out input characteristics that have more close relationship to the fault.

## I. INTRODUCTION

Once there are failure test cases reported in input-domain testing, input-level fault localization technique aims to find out characteristics of failure test cases.

To describe the characteristics, a model of minimal failure-causing schema was proposed [1]. Considering a boolean expression:  $a \wedge (\neg b \vee \neg c) \wedge d \vee e$ , and a clause disjunction fault (CDF) mutant:  $a \wedge (\neg b \vee \neg c) \wedge d \vee (d \vee e)$  [2]. There are total 5 failure test cases. In all 7 failure-causing schemas, (- 1 1 1 0) and (0 - - 1 0) are minimal ones. They predict that all 5 input variables are involved in the fault. But factually, only  $d$  and  $e$  are related to this fault, where  $e$  is replaced by  $d \vee e$ .

	$a$	$b$	$c$	$d$	$e$
$test_1$	0	0	0	1	0
$test_2$	0	0	1	1	0
$test_3$	0	1	0	1	0
$test_4$	0	1	1	1	0
$test_5$	1	1	1	1	0

  

	$a$	$b$	$c$	$d$	$e$
$schema_1$	0	0	0	1	0
$schema_2$	0	0	1	1	0
$schema_3$	0	1	0	1	0
$schema_4$	0	1	1	1	0
$schema_5$	1	1	1	1	0
$schema_6$	-	1	1	1	0
$schema_7$	0	-	-	1	0

In this paper, we propose a model of probabilistic failure-causing schema to describe this phenomena.

## II. PROBABILISTIC FAILURE-CAUSING SCHEMA

Considering a program under test with  $n$  input variables, each variable has a value set  $V_i$  ( $i = 1, 2, \dots, n$ ). The input domain of program is  $D = V_1 \times V_2 \times \dots \times V_n$ .

**Definition 1** (test case). A test case is a  $n$ -tuple ( $v_1 \in V_1, v_2 \in V_2, \dots, v_n \in V_n$ ).

**Definition 2** (schema). A  $k$ -value schema (or called a schema with strength  $k$ )  $s$  is a  $n$ -tuple ( $-, \dots, -, v_{i,1}, -, \dots, -, v_{i,2}, -, \dots, -, v_{i,k}, -, \dots, -$ ) where  $1 \leq k \leq n$ . Where, the values of  $k$  variables have been fixes, while the values of other  $n - k$  variables have not been fixed as denoted as "-".

**Definition 5** (probabilistic failure-causing schema). A  $k$ -value schema is a  $k$ -value probabilistic failure-causing schema with a failure probability  $p_{fail}$ , if the ratio of the number of failure test cases that contain such schema to the number of test cases that contain such schema is  $p_{fail}$ .

A schema with failure probability  $p_{fail}$  means that, for arbitrary test case  $t \in D = V_1 \times V_2 \times \dots \times V_n$  that contains such schema, the probability that  $t$  is a failure one is  $p_{fail}$ .

**Definition 6** (coverage probability). The coverage probability  $p_{cov}$  of a schema is the ratio of the number of test cases that contain such schema to the number of all test cases.

A schema with coverage probability  $p_{cov}$  means that, for arbitrary test case  $t \in D = V_1 \times V_2 \times \dots \times V_n$ , the probability that  $t$  contains such schema is  $p_{cov}$ . There is negative correlation between the coverage probability and the strength of schema

## III. APPROACH

People need characterize schemas with both higher failure probability and higher coverage probability, since the more  $p_{fail}$  means there is closer relationship between the schema and the fault, and the the more  $p_{cov}$  predicts less input variables that may be concerned with fault. By define a metric:

$$score(s) = p_{cov}(s) \times p_{fail}(s)$$

We can select probabilistic failure-causing schemas with the greatest score in input-level fault localization.

For previous example, we calculate  $p_{fail}$  and  $p_{cov}$  for each schema in 5 failure test cases (see Fig. 1). Three probabilistic failure-causing schemas with the greatest scores include:

$$\begin{aligned} score(- - - 1 0) &= \frac{1}{4} \times \frac{5}{8} = \frac{5}{32} \\ score(- - - 1 -) &= \frac{1}{2} \times \frac{5}{16} = \frac{5}{32} \\ score(- - - - 0) &= \frac{1}{2} \times \frac{5}{16} = \frac{5}{32} \end{aligned}$$

They predict that 2 variables  $d$  and  $e$  are involved in the fault.

$p_{cov}=1/32$	00010	00110	01010	01110	11110	$p_{fail}=1$
$p_{cov}=1/16$	-1110	0-010	0-110	00-10	01-10	-0010
$p_{cov}=1/8$	0--10	-1-10	--110	-11-	-11-0	...
$p_{cov}=1/4$	0--0	--10	0--0	0--1-	...	...
$p_{cov}=1/2$	---0	---1-	0---	-1--	-1---	1---

Fig. 1. Probabilistic failure-causing schemas (only some with greate  $p_{fail}$ )

## IV. CONCLUSION

A model of probabilistic failure-causing schema in input-domain testing is proposed. A simple example shows that they could reveal the source of faults more precision. More experiments are required in future works.

## REFERENCES

- [1] C. Nie, H. Leung. The Minimal Failure-causing Schema of Combinatorial Testing. ACM Transactions on Software Engineering and Methodology (TOSEM), 2011, 20(4): 15.
- [2] Z. Chen, T. Y. Chen, B. Xu. A Revisit of Fault Class Hierarchies in General Boolean Specifications. ACM Transactions on Software Engineering Methodology (TOSEM), 2011, 20(3).